

L8-5 Volume of Pyramids

Prisms

(has 3 times
the volume of
a pyramid)

$$V = Bh$$

cube/rectangular

$$V = (bh)h$$

triangular

$$V = \left(\frac{bh}{2}\right)h$$

cylinder

$$V = (\pi r^2)h$$

Pyramids

$$V = \frac{1}{3} Bh \rightarrow \begin{array}{l} \text{height} \\ \text{pyramid} \end{array}$$

area of base

square pyramid

$$V = \frac{1}{3} (b \cdot h) h \rightarrow \begin{array}{l} \text{height} \\ \text{of} \\ \text{pyramid} \end{array}$$

area of base

triangular pyramid

$$V = \frac{1}{3} \left(\frac{bh}{2}\right)h$$

$$\frac{1}{2} \cdot \frac{1}{3} = \frac{1}{6} (bh)h$$

cone

$$V = \frac{1}{3} (\pi r^2)h$$

What You'll Learn

Scan the lesson. Write the definitions of lateral face and pyramid.

- lateral face faces that meet @ the vertex at the top. (not the base)
- pyramid 3-d object w/ polygon base & triangular faces that meet @ a vertex at top

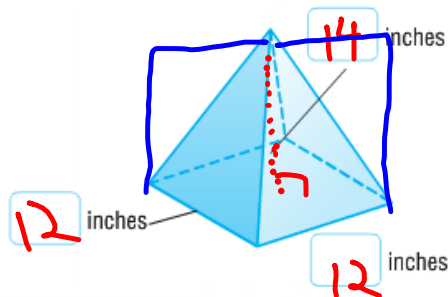
(vertex on a cone is actually an apex)



Real-World Link

Sand Sculpture Dion is helping his mother build a sand sculpture at the beach in the shape of a pyramid. The square pyramid has a base with a length and width of 12 inches each and a height of 14 inches.

1. Label the dimensions of the sand sculpture on the square pyramid below.



2. What is the area of the base of the pyramid?

$$12 \cdot 12 = 144 \text{ in}^2$$

3. What is the volume of a square prism with the same dimensions as the pyramid?

$$14 \cdot (12 \cdot 12) = 2016 \text{ in}^3$$

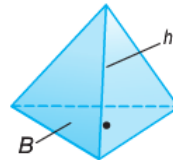
The pyramid Dion & his mother built has a volume of 672 in^3 .

$$\frac{2016}{3} = 672$$

Volume of a Pyramid

Words The volume V of a pyramid is one third the area of the base B times the height of the pyramid h .

Model



Symbols $V = \frac{1}{3}Bh$

Got It? Do this problem to find out.

- a. Find the volume of a pyramid that has a height of 9 centimeters and a rectangular base with a length of 7 centimeters and a width of 3 centimeters.



rectangular pyramid

$$\begin{aligned}
 V &= \frac{1}{3}Bh \\
 &= \frac{1}{3}(b \cdot l)h \\
 &= \frac{1}{3}(7 \cdot 3)9 \\
 &= \frac{1}{3}(189) = \frac{189}{3}
 \end{aligned}$$

$$= 63 \text{ cm}^3$$



Find the Height of a Pyramid

You can also use the formula for the volume of a pyramid to find a missing height.

Got It? Do these problems to find out.

- b. A triangular pyramid has a volume of 840 cubic inches. It has a base of 20 inches and a height of 21 inches. Find the height of the pyramid.
- c. A rectangular pyramid has a volume of 525 cubic feet. It has a base of 25 feet by 18 feet. Find the height of the pyramid.



$$V = 840 \text{ in}^3$$

$$V = \frac{1}{6} (\overset{\text{Base}}{b \cdot h}) h \rightarrow \text{Pyramidal}$$

$$840 = \frac{1}{6} (20 \cdot 21) h \quad \frac{420}{1} \cdot \frac{1}{6}$$

$$840 = \frac{420}{6} h \quad \leftarrow \quad 420 \div 6$$

$$\frac{840}{70} = \frac{70h}{70} \rightarrow 70 \cdot h$$

$$12 \text{ in.} = h$$

The height of the pyramid is 12 in.

Got It? Do these problems to find out.

- b. A triangular pyramid has a volume of 840 cubic inches. It has a base of 20 inches and a height of 21 inches. Find the height of the pyramid.
- c. A rectangular pyramid has a volume of 525 cubic feet. It has a base of 25 feet by 18 feet. Find the height of the pyramid.

$$V = \frac{1}{3} (\underbrace{b \cdot h}_{\text{base}}) h \rightarrow \text{height of pyramid}$$

$$525 = \frac{1}{3} (25 \cdot 18) h$$

$$525 = \frac{1}{3} (450) h$$

$$525 = \frac{450}{3} h$$

$$\frac{525}{150} = \frac{150}{150} h$$

$$3.5 \text{ ft} = h$$

The pyramid is 3.5 feet tall.

5. The Transamerica Pyramid is a skyscraper in San Francisco. The rectangular base has a length of 175 feet and a width of 120 feet. The height is 853 feet.

Find the volume of the building. (Example 5) _____

rectangular pyramid

$$\begin{aligned} V &= \frac{1}{3}(b \cdot h)h \\ &= \frac{1}{3}(175 \cdot 120)853 \\ &= \frac{1}{3}(21000)853 \end{aligned}$$

$$= \frac{21000}{3} \cdot 853$$

$$= 7000 \cdot 853$$

$$= 5,971,000 \text{ ft}^3$$

